# JEE MAIN + ADVANCED MATHEMATICS 

# TOPIC NAME <br> CIRCLE 

(PRACTICE SHEET)

## LEVEL-1

## Question

## Standard forms of Equation of a Circle

Q. 1 The length of the diameter of the circle $x^{2}+y^{2}-4 x-6 y+4=0$ is -
(A) 9
(B) 3
(C) 4
(D) 6

If $(x, 3)$ and $(3,5)$ are the extremities of a diameter of a circle with centre at $(2, y)$. Then the value of $x$ and $y$ are-
(A) $\mathrm{x}=1, \mathrm{y}=4$
(B) $x=4, y=1$
(C) $x=8, y=2$
(D) None of these
Q. 8 If $(0,1)$ and $(1,1)$ are end points of a diameter of a circle, then its equation is-
(A) $x^{2}+y^{2}-x-2 y+1=0$
(B) $x^{2}+y^{2}+x-2 y+1=0$
(C) $x^{2}+y^{2}-x-2 y-1=0$
(D) None of these
Q. 9 The coordinates of any point on the circle $x^{2}+y^{2}=4$ are-
(A) $(\cos \alpha, \sin \alpha)$
(B) $(4 \cos \alpha, 4 \sin \alpha)$
(C) $(2 \cos \alpha, 2 \sin \alpha)$
(D) $(\sin \alpha, \cos \alpha)$
Q. 10 The parametric coordinates of any point on the circle $x^{2}+y^{2}-4 x-4 y=0$ are-
(A) $(-2+2 \cos \alpha,-2+2 \sin \alpha)$
(B) $(2+2 \cos \alpha, 2+2 \sin \alpha)$
(C) $(2+2 \sqrt{2} \cos \alpha, 2+2 \sqrt{2} \sin \alpha)$
(D) None of these
Q. 11 The parametric coordinates of a point on the circle $x^{2}+y^{2}-2 x+2 y-2=0$ are -
(A) $(1-2 \cos \alpha, 1-2 \sin \alpha)$
(B) $(1+2 \cos \alpha, 1+2 \sin \alpha)$
(C) $(1+2 \cos \alpha,-1+2 \sin \alpha)$
(D) $(-1+2 \cos \alpha, 1+2 \sin \alpha)$
Q. 12 The equation $k\left(x^{2}+y^{2}\right)-x-y+k=0$ represents a real circle, if-
(A) $\mathrm{k}<\sqrt{2}$
(B) $k>\sqrt{2}$
(C) $\mathrm{k}>1 / \sqrt{2}$
(D) $0<|\mathbf{k}| \leq \frac{1}{\sqrt{2}}$
(A) $\sqrt{(a-g)^{2}+b^{2}}$
(B) $\sqrt{a^{2}+(b+g)^{2}}$
(C) $\sqrt{a^{2}+(b-g)^{2}}$
(D) $\sqrt{(a+g)^{2}+b^{2}}$
Q. 13 If the equation
$p x^{2}+(2-q) x y+3 y^{2}-6 q x+30 y+6 q=0$ represents a circle, then the values of $p$ and $q$ are -
(A) 2, 2
(B) 3,1
(C) 3, 2
(D) 3, 4
Q. 14 The circle represented by the equation $x^{2}+y^{2}+2 g x+2 f y+c=0$ will be a point circle, if-
(A) $g^{2}+f^{2}=c$
(B) $g^{2}+f^{2}+c=0$
(C) $g^{2}+f^{2}>c$
(D) None of these
Q. 15 The equation of the circum-circle of the triangle formed by the lines $x=0, y=0, \frac{x}{a}-\frac{y}{b}=1$, is -
(A) $x^{2}+y^{2}+a x-b y=0$
(B) $x^{2}+y^{2}-a x+b y=0$
(C) $x^{2}+y^{2}-a x-b y=0$
(D) $x^{2}+y^{2}+a x+b y=0$
Q. 16 The circum-circle of the quadrilateral formed by the lines $x=a, x=2 a, y=-a, y=a$ is-
(A) $x^{2}+y^{2}-3 a x-a^{2}=0$
(B) $x^{2}+y^{2}+3 a x+a^{2}=0$
(C) $x^{2}+y^{2}-3 a x+a^{2}=0$
(D) $x^{2}+y^{2}+3 a x-a^{2}=0$
Q. 17 The x coordinates of two points A and B are roots of equation $x^{2}+2 x-a^{2}=0$ and $y$ coordinate are roots of equation $y^{2}+4 y-b^{2}=0$ then equation of the circle which has diameter AB is-
(A) $(x-1)^{2}+(y-2)^{2}=5+a^{2}+b^{2}$
(B) $(x+1)^{2}+(y+2)^{2}=\sqrt{\left(5+a^{2}+b^{2}\right)}$
(C) $(x+1)^{2}+(y+2)^{2}=\left(a^{2}+b^{2}\right)$
(D) $(x+1)^{2}+(y+2)^{2}=5+a^{2}+b^{2}$

## Question

based on

## Equation of Circle in special cases

Q. 18 A circle touches both the axes and its centre lies in the fourth quadrant. If its radius is 1 then its equation will be -
(A) $x^{2}+y^{2}-2 x+2 y+1=0$
(B) $x^{2}+y^{2}+2 x-2 y-1=0$
(C) $x^{2}+y^{2}-2 x-2 y+1=0$
(D) $x^{2}+y^{2}+2 x-2 y+1=0$
Q. 19 The equation to a circle with centre $(2,1)$ and touching x axis is -
(A) $x^{2}+y^{2}+4 x+2 y+4=0$
(B) $x^{2}+y^{2}-4 x-2 y+4=0$
(C) $x^{2}+y^{2}-4 x-2 y+1=0$
(D) None of these
Q. 20 The equation to the circle whose radius is 4 and which touches the x -axis at a distance -3 from the origin is-
(A) $x^{2}+y^{2}-6 x+8 y-9=0$
(B) $x^{2}+y^{2} \pm 6 x-8 y+9=0$
(C) $x^{2}+y^{2}+6 x \pm 8 y+9=0$
(D) $x^{2}+y^{2} \pm 6 x-8 y-9=0$
Q. 21 The equation of the circle touching the lines $x=0, y=0$ and $x=2 c$ is-
(A) $x^{2}+y^{2}+2 c x+2 c y+c^{2}=0$
(B) $x^{2}+y^{2}-2 c x+2 c y+c^{2}=0$
(C) $x^{2}+y^{2} \pm 2 c x-2 c y+c^{2}=0$
(D) $x^{2}+y^{2}-2 c x \pm 2 c y+c^{2}=0$
Q. 22 The circle $x^{2}+y^{2}-4 x-4 y+4=0$ is-
(A) touches $x$-axes only
(B) touches both axes
(C) passes through the origin
(D) touches y-axes only
Q. 23 If a be the radius of a circle which touches $x$-axis at the origin, then its equation is-
(A) $x^{2}+y^{2}+a x=0$
(B) $x^{2}+y^{2} \pm 2 y a=0$
(C) $x^{2}+y^{2} \pm 2 x a=0$
(D) $x^{2}+y^{2}+y a=0$
Q. 24 The point where the line $x=0$ touches the circle $x^{2}+y^{2}-2 x-6 y+9=0$ is-
(A) $(0,1)$
(B) $(0,2)$
(C) $(0,3)$
(D) No where
Q. 25 Circle $x^{2}+y^{2}+6 y=0$ touches -
(A) $x$-axis at the point $(3,0)$
(B) $x$-axis at the origin
(C) $y$-axis at the origin
(D) The line $y+3=0$

## Question <br> based on

## Position of Point w.r.t. Circle

Q. 26 Position of the point $(1,1)$ with respect to the circle $x^{2}+y^{2}-x+y-1=0$ is -
(A) Outside the circle
(B) Inside the circle
(C) Upon the circle
(D) None of these
Q. 27 The point $(0.1,3.1)$ with respect to the circle $x^{2}+y^{2}-2 x-4 y+3=0$, is -
(A) Inside the circle but not at the centre
(B) At the centre of the circle
(C) On the circle
(D) Outside the circle

## Question <br> based on

## Line \& Circle

Q. 28 The straight line $(x-2)+(y+3)=0$ cuts the circle $(x-2)^{2}+(y-3)^{2}=11$ at-
(A) no points
(B) two points
(C) one point
(D) None of these
Q. 29 If the line $3 x+4 y=m$ touches the circle $x^{2}+y^{2}=10 x$, then $m$ is equal to-
(A) 40,10
(B) $40,-10$
(C) $-40,10$
(D) $-40,-10$
Q. 30 Circle $x^{2}+y^{2}-4 x-8 y-5=0$ will intersect the line $3 x-4 y=m$ in two distinct points, if -
(A) $-10<$ m $<5$
(B) $9<\mathrm{m}<20$
(C) $-35<$ m $<15$
(D) None of these
Q. 31 The length of the intercept made by the circle $x^{2}+y^{2}=1$ on the line $x+y=1$ is-
(A) $1 / \sqrt{2}$
(B) $\sqrt{2}$
(C) 2
(D) $2 \sqrt{2}$
Q. 32 If a circle with centre $(0,0)$ touches the line $5 x+12 y=1$ then its equation will be-
(A) $13\left(x^{2}+y^{2}\right)=1$
(B) $x^{2}+y^{2}=169$
(C) $169\left(x^{2}+y^{2}\right)=1$
(D) $x^{2}+y^{2}=13$
Q. 33 The equation of circle which touches the axes of coordinates and the line $\frac{x}{3}+\frac{y}{4}=1$ and whose centre lies in the first quadrant is $\mathrm{x}^{2}+\mathrm{y}^{2}-2 \mathrm{cx}-2 \mathrm{cy}+\mathrm{c}^{2}=0$, where c is-
(A) 2
(B) 0
(C) 3
(D) 6
Q. 34 For the circle $x^{2}+y^{2}-2 x+4 y-4=0$, the line $2 x-y+1=0$ is a-
(A) chord
(B) diameter
(C) tangent line
(D) None of these
Q. 35 The line $y=x+c$ will intersect the circle $x^{2}+y^{2}=1$ in two coincident points, if-
(A) $\mathrm{c}=-\sqrt{2}$
(B) $\mathrm{c}=\sqrt{2}$
(C) $\mathrm{c}= \pm \sqrt{2}$
(D) None of these
Q. 36 Centre of a circle is (2, 3). If the line $x+y=1$ touches it. Find the equation of circle-
(A) $x^{2}+y^{2}-4 x-6 y+5=0$
(B) $x^{2}+y^{2}-4 x-6 y-4=0$
(C) $x^{2}+y^{2}-4 x-6 y-5=0$
(D) None of these
Q. 37 The lines $12 x-5 y-17=0$ and $24 x-10 y+44=0$ are tangents to the same circle. Then the radius of the circle is-
(A) 1
(B) $1 \frac{1}{2}$
(C) 2
(D) None of these
Q. 38 If the circle $x^{2}+y^{2}=a^{2}$ cuts off a chord of length $2 b$ from the line $y=m x+c$, then-
(A) $\left(1-\mathrm{m}^{2}\right)\left(\mathrm{a}^{2}-\mathrm{b}^{2}\right)=\mathrm{c}^{2}$
(B) $\left(1+\mathrm{m}^{2}\right)\left(\mathrm{a}^{2}-\mathrm{b}^{2}\right)=\mathrm{c}^{2}$
(C) $\left(1-\mathrm{m}^{2}\right)\left(\mathrm{a}^{2}+\mathrm{b}^{2}\right)=\mathrm{c}^{2}$
(D) None of these

## Question <br> based on <br> Equation of Tangent \& Normal

Q. $39 \ell \mathrm{x}+\mathrm{my}+\mathrm{n}=0$ is a tangent line to the circle $x^{2}+y^{2}=r^{2}$, if-
(A) $\ell^{2}+\mathrm{m}^{2}=\mathrm{n}^{2} \mathrm{r}^{2}$
(B) $\ell^{2}+\mathrm{m}^{2}=\mathrm{n}^{2}+\mathrm{r}^{2}$
(C) $\mathrm{n}^{2}=\mathrm{r}^{2}\left(\ell^{2}+\mathrm{m}^{2}\right)$
(D) None of these
Q. 40 The equation of the tangent to the circle $x^{2}+y^{2}=25$ which is inclined at $60^{\circ}$ angle with x -axis, will be-
(A) $y=\sqrt{3} x \pm 10$
(B) $y=\sqrt{3} x \pm 2$
(C) $\sqrt{3} y=x \pm 10$
(D) None of these
Q. 41 The gradient of the tangent line at the point $(a \cos \alpha, a \sin \alpha)$ to the circle $x^{2}+y^{2}=a^{2}$, is-
(A) $\tan (\pi-\alpha)$
(B) $\tan \alpha$
(C) $\cot \alpha$
(D) $-\cot \alpha$
Q. 42 If $y=c$ is $a$ tangent to the circle $x^{2}+y^{2}-2 x+2 y-2=0$ at $(1,1)$, then the value of c is-
(A) 1
(B) 2
(C) -1
(D) -2
Q. 43 Line $3 x+4 y=25$ touches the circle $x^{2}+y^{2}=25$ at the point-
(A) $(4,3)$
(B) $(3,4)$
(C) $(-3,-4)$
(D) None of these
Q. 44 The equations of the tangents drawn from the point $(0,1)$ to the circle $x^{2}+y^{2}-2 x+4 y=0$ are-
(A) $2 x-y+1=0, x+2 y-2=0$
(B) $2 x-y-1=0, x+2 y-2=0$
(C) $2 x-y+1=0, x+2 y+2=0$
(D) $2 x-y-1=0, x+2 y+2=0$
Q. 45 The tangent lines to the circle $x^{2}+y^{2}-6 x+4 y=12$ which are parallel to the line $4 x+3 y+5=0$ are given by-
(A) $4 x+3 y-7=0,4 x+3 y+15=0$
(B) $4 x+3 y-31=0,4 x+3 y+19=0$
(C) $4 x+3 y-17=0,4 x+3 y+13=0$
(D) None of these
Q. 46 The equations of tangents to the circle $\mathrm{x}^{2}+\mathrm{y}^{2}-22 \mathrm{x}-4 \mathrm{y}+25=0$ which are perpendicular to the line $5 x+12 y+8=0$ are-
(A) $12 \mathrm{x}-5 \mathrm{y}+8=0,12 \mathrm{x}-5 \mathrm{y}=252$
(B) $12 x-5 y-8=0,12 x-5 y+252=0$
(C) $12 x-5 y=0,12 x-5 y=252$
(D) None of these
Q. 47 The equation of the normal to the circle $x^{2}+y^{2}=9$ at the point $\left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$ is-
(A) $x-y=\frac{\sqrt{2}}{3}$
(B) $x+y=0$
(C) $x-y=0$
(D) None of these
Q. 48 The equation of the normal at the point $(4,-1)$ of the circle $x^{2}+y^{2}-40 x+10 y=153$ is-
(A) $x+4 y=0$
(B) $4 x+y=3$
(C) $x-4 y=0$
(D) $4 x-y=0$
Q. 49 The equation of the normal to the circle $x^{2}+y^{2}-8 x-2 y+12=0$ at the points whose ordinate is -1 , will be-
(A) $2 \mathrm{x}-\mathrm{y}-7=0,2 \mathrm{x}+\mathrm{y}-9=0$
(B) $2 \mathrm{x}+\mathrm{y}-7=0,2 \mathrm{x}+\mathrm{y}+9=0$
(C) $2 x+y+7=0,2 x+y+9=0$
(D) $2 x-y+7=0,2 x-y+9=0$
Q. 50 The line $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0$ is a normal to the circle $x^{2}+y^{2}=r^{2}$. The portion of the line $a x+b y+c=0$ intercepted by this circle is of length-
(A) $r^{2}$
(B) $r$
(C) 2 r
(D) $\sqrt{\mathrm{r}}$

## Question <br> based on <br> Length of Tangent \& Pair of Tangents

Q. 51 If the length of tangent drawn from the point $(5,3)$ to the circle $x^{2}+y^{2}+2 x+k y+17=0$ is 7 , then $\mathrm{k}=$
(A) -6
(B) -4
(C) 4
(D) $13 / 2$
Q. 52 The length of tangent from the point $(5,1)$ to the circle $x^{2}+y^{2}+6 x-4 y-3=0$, is-
(A) 29
(B) 81
(C) 7
(D) 21
Q. 53 The length of the tangent drawn from the point $(2,3)$ to the circle $2\left(x^{2}+y^{2}\right)-7 x+9 y-11=0$
(A) 18
(B) 14
(C) $\sqrt{14}$
(D) $\sqrt{28}$
Q. 54 If the lengths of the tangents drawn from the point $(1,2)$ to the circles $x^{2}+y^{2}+x+y-4=0$ and $3 x^{2}+3 y^{2}-x-y+k=0$ be in the ratio $4: 3$, then $\mathrm{k}=$
(A) $21 / 2$
(B) $7 / 2$
(C)-21/4
(D) $7 / 4$
Q. 55 A pair of tangents are drawn from the origin to the circle $\mathrm{x}^{2}+\mathrm{y}^{2}+20(\mathrm{x}+\mathrm{y})+20=0$. The equation of the pair of tangents is-
(A) $x^{2}+y^{2}+5 x y=0$
(B) $x^{2}+y^{2}+10 x y=0$
(C) $2 x^{2}+2 y^{2}+5 x y=0$
(D) $2 x^{2}+2 y^{2}-5 x y=0$
Q. 56 If the equation of one tangent to the circle with centre at $(2,-1)$ from the origin is $3 x+y=0$, then the equation of the other tangent through the origin is-
(A) $x+3 y=0$
(B) $3 x-y=0$
(C) $x-3 y=0$
(D) $x+2 y=0$
Q. 57 The equation of the pair of tangents drawn to the circle $x^{2}+y^{2}-2 x+4 y+3=0$ from $(6,-5)$ is-
(A) $7 x^{2}+23 y^{2}+30 x y+66 x+50 y-73=0$
(B) $7 x^{2}+23 y^{2}-30 x y-66 x-50 y+73=0$
(C) $7 x^{2}+23 y^{2}+30 x y-66 x-50 y-73=0$
(D) None of these
Q. 58 The angle between the tangents drawn from the origin to the circle $(x-7)^{2}+(y+1)^{2}=25$ is-
(A) $\pi / 3$
(B) $\pi / 6$
(C) $\pi / 2$
(D) $\pi / 8$

## Question <br> based on <br> Chord of Contact

Q. 59 The equation of the chord of contact of the circle $x^{2}+y^{2}+4 x+6 y-12=0$ with respect to the point $(2,-3)$ is-
(A) $4 x=17$
(B) $4 x+y=17$
(C) $4 y=17$
(D) None of these
Q. 60 The equation of the chord of contact, if the tangents are drawn from the point $(5,-3)$ to the circle $x^{2}+y^{2}=10$, is-
(A) $5 x-3 y=10$
(B) $3 x+5 y=10$
(C) $5 x+3 y=10$
(D) $3 x-5 y=10$

## Question

based on

## Director Circle

Q. 61 The equation of director circle to the circle $x^{2}+y^{2}=8$ is-
(A) $x^{2}+y^{2}=8$
(B) $x^{2}+y^{2}=16$
(C) $x^{2}+y^{2}=4$
(D) $x^{2}+y^{2}=12$
Q. 62 Two perpendicular tangents to the circle $x^{2}+y^{2}=a^{2}$ meet at $P$. Then the locus of $P$ has the equation-
(A) $x^{2}+y^{2}=2 a^{2}$
(B) $x^{2}+y^{2}=3 a^{2}$
(C) $x^{2}+y^{2}=4 a^{2}$
(D) None of these

## Question

based on

## Position of Two Circle

Q. 63 Consider the circle $x^{2}+(y-1)^{2}=9$, $(x-1)^{2}+y^{2}=25$. They are such that-
(A) each of these circles lies outside the other
(B) one of these circles lies entirely inside the other
(C) these circles touch each other
(D) they intersect in two points
Q. 64 Circles $x^{2}+y^{2}-2 x-4 y=0$ and $x^{2}+y^{2}-8 y-4=0$
(A) touch each other internally
(B) cuts each other at two points
(C) touch each other externally
(D) None of these
Q. 65 The number of common tangents of the circle $\mathrm{x}^{2}+\mathrm{y}^{2}-2 \mathrm{x}-1=0$ and $\mathrm{x}^{2}+\mathrm{y}^{2}-2 \mathrm{y}-7=0$ is-
(A) 1
(B) 3
(C) 2
(D) 4
Q. 66 If the circles $x^{2}+y^{2}+2 x-8 y+8=0$ and $x^{2}+y^{2}+10 x-2 y+22=0$ touch each other, their point of contact is-
(A) $\left(-\frac{17}{5}, \frac{11}{5}\right)$
(B) $\left(\frac{11}{3}, 2\right)$
(C) $\left(\frac{17}{5}, \frac{11}{5}\right)$
(D) $\left(-\frac{11}{3}, 2\right)$
Q. 67 For the given circles $x^{2}+y^{2}-6 x-2 y+1=0$ and $x^{2}+y^{2}+2 x-8 y+13=0$, which of the following is true-
(A) one circle lies completely outside the other
(B) one circle lies inside the other
(C) two circle intersect in two points
(D) they touch each other
Q. 68 If circles $x^{2}+y^{2}=r^{2}$ and $x^{2}+y^{2}-20 x+36=0$ intersect at real and different points, then-
(A) $\mathrm{r}<2$ and $\mathrm{r}>18$
(B) $2<r<18$
(C) $r=2$ and $r=18$
(D) None of these
Q. 69 The number of common tangents that can be drawn to the circles $x^{2}+y^{2}-4 x-6 y-3=0$ and $x^{2}+y^{2}+2 x+2 y+1=0$ is-
(A) 1
(B) 2
(C) 3
(D) 4

## Question <br> Equation of a chord whose middle point is given

Q. 70 Find the locus of mid point of chords of circle $x^{2}+y^{2}=25$ which subtends right angle at origin-
(A) $x^{2}+y^{2}=25 / 4$
(B) $x^{2}+y^{2}=5$
(C) $x^{2}+y^{2}=25 / 2$
(D) $x^{2}+y^{2}=5 / 2$
Q. 71 The equation to the chord of the circle $x^{2}+y^{2}=16$ which is bisected at $(2,-1)$ is-
(A) $2 x+y=16$
(B) $2 x-y=16$
(C) $x+2 y=5$
(D) $2 x-y=5$
Q. 72 The equation of the chord of the circle $x^{2}+y^{2}-6 x+8 y=0$ which is bisected at the point $(5,-3)$ is-
(A) $2 x-y+7=0$
(B) $2 x+y-7=0$
(C) $2 x+y+7=0$
(D) $2 x-y-7=0$

## Question <br> based on <br> Circle through the Point of Intersection

Q. 73 The equation of the circle passing through the point $(1,1)$ and through the point of intersection of circles $x^{2}+y^{2}+13 x-3 y=0$ and $2 x^{2}+2 y^{2}+4 x-7 y-25=0$ is-
(A) $4 x^{2}+4 y^{2}-17 x-10 y+25=0$
(B) $4 x^{2}+4 y^{2}+30 x-13 y-25=0$
(C) $4 x^{2}+4 y^{2}-30 x-10 y-25=0$
(D) None of these
Q. 74 The equation of circle passing through the points of intersection of circles $x^{2}+y^{2}=6$ and $x^{2}+y^{2}-6 x+8=0$ and the point $(1,1)$ is-
(A) $x^{2}+y^{2}-4 y+2=0$
(B) $x^{2}+y^{2}-3 x+1=0$
(C) $x^{2}+y^{2}-6 x+4=0$
(D) None of these
Q. 75 The equation of the circle whose diameter is the common chord of the circles $x^{2}+y^{2}+3 x+2 y+1=0$ and $x^{2}+y^{2}+3 x+4 y+2=0$ is-
(A) $x^{2}+y^{2}+3 x+y+5=0$
(B) $x^{2}+y^{2}+x+3 y+7=0$
(C) $x^{2}+y^{2}+2 x+3 y+1=0$
(D) $2\left(x^{2}+y^{2}\right)+6 x+2 y+1=0$

## Question <br> based on

## Common chord of two Circles

Q. 76 The common chord of $x^{2}+y^{2}-4 x-4 y=0$ and $x^{2}+y^{2}=16$ subtends at the origin an angle equal to-
(A) $\pi / 6$
(B) $\pi / 4$
(C) $\pi / 3$
(D) $\pi / 2$
Q. 77 The distance from the centre of the circle $x^{2}+y^{2}=2 x$ to the straight line passing through the points of intersection of the two circles $x^{2}+y^{2}+5 x-8 y+1=0, x^{2}+y^{2}-3 x+7 y-25=0$ is-
(A) 1
(B) 2
(C) 3
(D) None of these
Q. 78 The length of the common chord of the circle $x^{2}+y^{2}+4 x+6 y+4=0$ and $x^{2}+y^{2}+6 x+4 y+4=0$ is-
(A) $\sqrt{10}$
(B) $\sqrt{22}$
(C) $\sqrt{34}$
(D) $\sqrt{38}$
Q. 79 The length of the common chord of circle $x^{2}+y^{2}-6 x-16=0$ and $x^{2}+y^{2}-8 y-9=0$ is-
(A) $10 \sqrt{3}$
(B) $5 \sqrt{3}$
(C) $5 \sqrt{3} / 2$
(D) None of these
Q. 80 Length of the common chord of the circles $x^{2}+y^{2}+5 x+7 y+9=0$ and $x^{2}+y^{2}+7 x+5 y+9=0$ is-
(A) 8
(B) 9
(C) 7
(D) 6

## Question based on

## Angle of intersection of two Circles

Q. 81 Two given circles $x^{2}+y^{2}+a x+b y+c=0$ and $x^{2}+y^{2}+d x+e y+f=0$ will intersect each other orthogonally, only when-
(A) $a d+b e=c+f$
(B) $a+b+c=d+e+f$
(C) $\mathrm{ad}+\mathrm{be}=2 \mathrm{c}+2 \mathrm{f}$
(D) $2 \mathrm{ad}+2 \mathrm{be}=\mathrm{c}+\mathrm{f}$
Q. 82 If the circles of same radius a and centres at $(2,3)$ and $(5,6)$ cut orthogonally, then a is equal to-
(A) 6
(B) 4
(C) 3
(D) 10
Q. 83 The angle of intersection of circles $x^{2}+y^{2}+8 x$ $-2 y-9=0$ and $x^{2}+y^{2}-2 x+8 y-7=0$ is -
(A) $60^{\circ}$
(B) $90^{\circ}$
(C) $45^{\circ}$
(D) $30^{\circ}$
Q. 84 The angle of intersection of two circles is $0^{\circ}$ if -
(A) they are separate
(B) they intersect at two points
(C) they intersect only at a single point
(D) it is not possible
Q. 85 If a circle passes through the point $(1,2)$ and cuts the circle $x^{2}+y^{2}=4$ orthogonally, then the equation of the locus of its centre is -
(A) $x^{2}+y^{2}-2 x-6 y-7=0$
(B) $x^{2}+y^{2}-3 x-8 y+1=0$
(C) $2 x+4 y-9=0$
(D) $2 x+4 y-1=0$
Q. 86 The equation of the circle which passes through the origin has its centre on the line $x+y=4$ and cuts the circle $x^{2}+y^{2}-4 x+2 y+4=0$ orthogonally, is -
(A) $x^{2}+y^{2}-2 x-6 y=0$
(B) $x^{2}+y^{2}-6 x-3 y=0$
(C) $x^{2}+y^{2}-4 x-4 y=0$
(D) None of these

## LEVEL-2

Q. 1 If $\theta$ is the angle subtended at $\mathrm{P}\left(\mathrm{x}_{1}, \mathrm{y}_{1}\right)$ by the circle $S \equiv x^{2}+y^{2}+2 g x+2 f y+c=0$ then -
(A) $\tan \theta=\frac{2 \sqrt{\mathrm{~g}^{2}+\mathrm{f}^{2}-\mathrm{c}}}{\sqrt{\mathrm{S}_{1}}}$
(B) $\cot \frac{\theta}{2}=\frac{\sqrt{\mathrm{S}_{1}}}{\sqrt{\mathrm{~g}^{2}+\mathrm{f}^{2}-\mathrm{c}}}$
(C) $\cot \theta=\frac{\sqrt{\mathrm{S}_{1}}}{\sqrt{\mathrm{~g}^{2}+\mathrm{f}^{2}-\mathrm{c}}}$
(D) None of these
Q. 2 The circle $(x-2)^{2}+(y-5)^{2}=a^{2}$ will be inside the circle $(x-3)^{2}+(y-6)^{2}=b^{2}$ if -
(A) $b>a+\sqrt{2}$
(B) $a<\sqrt{2}-b$
(C) $a-b<\sqrt{2}$
(D) $a+b>\sqrt{2}$
Q. 3 If the lines $a_{1} x+b_{1} y+c_{1}=0$ and $a_{2} x+b_{2} y+c_{2}=0$ cut the coordinate axes in concyclic points, then -
(A) $a_{1} a_{2}=b_{1} b_{2}$
(B) $a_{1} b_{1}=a_{2} b_{2}$
(C) $a_{1} b_{2}=a_{2} b_{1}$
(D) None of these
Q. 4 Four distinct points $(2 \mathrm{k}, 3 \mathrm{k}),(1,0),(0,1)$ and $(0,0)$ lie on a circle for -
(A) All integral values of k
(B) $0<\mathrm{k}<1$
(C) $\mathrm{k}<0$
(D) $5 / 13$
Q. 5 The circle $x^{2}+y^{2}+2 g x+2 f y+c=0$ bisects the circumference of the circle
$x^{2}+y^{2}+2 a x+2 b y+d=0$, then -
(A) $2 \mathrm{a}(\mathrm{g}-\mathrm{a})+2 \mathrm{~b}(\mathrm{f}-\mathrm{b})=\mathrm{c}-\mathrm{d}$
(B) $2 \mathrm{a}(\mathrm{g}+\mathrm{a})+2 \mathrm{~b}(\mathrm{f}+\mathrm{b})=\mathrm{c}+\mathrm{d}$
(C) $2 \mathrm{~g}(\mathrm{~g}-\mathrm{a})+2 \mathrm{f}(\mathrm{f}-\mathrm{b})=\mathrm{d}-\mathrm{c}$
(D) $2 g(g+a)+2 f(f+b)=c+d$
Q. 6 Three equal circles each of radius $r$ touch one another. The radius of the circle which touching by all the three given circles internally is -
(A) $(2+\sqrt{3}) \mathrm{r}$
(B) $\frac{(2+\sqrt{3})}{\sqrt{3}} r$
(C) $\frac{(2-\sqrt{3})}{\sqrt{3}} r$
(D) $(2-\sqrt{3}) \mathrm{r}$
Q. 7 The equation of the in-circle of the triangle formed by the axes and the line $4 x+3 y=6$ is -
(A) $x^{2}+y^{2}-6 x-6 y+9=0$
(B) $4\left(x^{2}+y^{2}-x-y\right)+1=0$
(C) $4\left(x^{2}+y^{2}+x+y\right)+1=0$
(D) None of these
Q. 8 The equation of circle passing through the points of intersection of circle $x^{2}+y^{2}=6$ and $x^{2}+y^{2}-6 x+8=0$ and the point $(1,1)$ is -
(A) $x^{2}+y^{2}-3 x+1=0$
(B) $x^{2}+y^{2}-6 x+4=0$
(C) $x^{2}+y^{2}-4 y+2=0$
(D) none of these
Q. 9 If the two circles $(x-1)^{2}+(y-3)^{2}=r^{2}$ and $x^{2}+y^{2}-8 x+2 y+8=0$ intersect in two distinct points then -
(A) $2<r<8$
(B) $\mathrm{r}<2$
(C) $r=2, r=8$
(D) $r>2$
Q. 10 If from any point $P$ on the circle $x^{2}+y^{2}+2 g x$ $+2 f y+c=0$, tangents are drawn to the circle $x^{2}+y^{2}+2 g x+2 f y+c \sin ^{2} \alpha+\left(g^{2}+f^{2}\right) \cos ^{2} \alpha=0$, then the angle between the tangents is -
(A) $\alpha$
(B) $2 \alpha$
(C) $\alpha / 2$
(D) None of these
Q. 11 The circles whose equations are $x^{2}+y^{2}+c^{2}=2 a x$ and $x^{2}+y^{2}+c^{2}-2 b y=0$ will touch one another externally if -
(A) $\frac{1}{\mathrm{~b}^{2}}+\frac{1}{\mathrm{c}^{2}}=\frac{1}{\mathrm{a}^{2}}$
(B) $\frac{1}{\mathrm{c}^{2}}+\frac{1}{\mathrm{a}^{2}}=\frac{1}{\mathrm{~b}^{2}}$
(C) $\frac{1}{\mathrm{a}^{2}}+\frac{1}{\mathrm{~b}^{2}}=\frac{1}{\mathrm{c}^{2}}$
(D) None of these
Q. 12 The possible values of $p$ for which the line $x \cos \alpha+y \sin \alpha=p$ is a tangent to the circle $x^{2}+y^{2}-2 q x \cos \alpha-2 q y \sin \alpha=0$ is/are -
(A) $q$ and $2 q$
(B) 0 and $q$
(C) 0 and $2 q$
(D) $q$
Q. 13 The length of the tangent drawn from any point on the circle $x^{2}+y^{2}+2 g x+2 f y+\alpha=0$ to the circle $x^{2}+y^{2}+2 g x+2 f y+\beta=0$ is -
(A) $\sqrt{\beta-\alpha}$
(B) $\sqrt{\alpha \beta}$
(C) $\sqrt{\alpha-\beta}$
(D) $\sqrt{(\alpha / \beta)}$
Q. 14 The locus of centre of the circle which cuts the circle $x^{2}+y^{2}=k^{2}$ orthogonally and passes through the point $(p, q)$ is -
(A) $2 \mathrm{px}+2 \mathrm{qy}-\left(\mathrm{p}^{2}+\mathrm{q}^{2}+\mathrm{k}^{2}\right)=0$
(B) $x^{2}+y^{2}-3 p x-4 q y-\left(p^{2}+q^{2}-k^{2}\right)=0$
(C) $2 p x+2 q y-\left(p^{2}-q^{2}+k^{2}\right)=0$
(D) $x^{2}+y^{2}-2 p x-3 q y-\left(p^{2}-q^{2}-k^{2}\right)=0$
Q. 15 If the line $(x+g) \cos \theta+(y+f) \sin \theta=k$ touches the circle $x^{2}+y^{2}+2 g x+2 f y+c=0$, then -
(A) $g^{2}+f^{2}=k^{2}+c^{2}$
(B) $\mathrm{g}^{2}+\mathrm{f}^{2}=\mathrm{k}+\mathrm{c}$
(C) $\mathrm{g}^{2}+\mathrm{f}^{2}=\mathrm{k}^{2}+\mathrm{c}$
(D) None of these
Q. 16 The locus of the point which moves so that the lengths of the tangents from it to two given concentric circles $x^{2}+y^{2}=a^{2}$ and $x^{2}+y^{2}=b^{2}$ are inversely as their radii has equation -
(A) $x^{2}+y^{2}=(a+b)^{2}$
(B) $x^{2}+y^{2}=a^{2}+b^{2}$
(C) $\left(a^{2}+b^{2}\right)\left(x^{2}+y^{2}\right)=1$
(D) $x^{2}+y^{2}=a^{2}-b^{2}$
Q. 17 The equation of the circle which passes through $(1,0)$ and $(0,1)$ and has its radius as small as possible, is -
(A) $2 x^{2}+2 y^{2}-3 x-3 y+1=0$
(B) $x^{2}+y^{2}-x-y=0$
(C) $x^{2}+y^{2}-2 x-2 y+1=0$
(D) $x^{2}+y^{2}-3 x-3 y+2=0$
Q. 18 The distance between the chords of contact of the tangents to the circle $x^{2}+y^{2}+2 g x+2 f y+c=0$ from the origin and from the point ( $\mathrm{g}, \mathrm{f}$ ) is -
(A) $g^{2}+f^{2}$
(B) $\frac{1}{2}\left(\mathrm{~g}^{2}+\mathrm{f}^{2}+\mathrm{c}\right)$
(C) $\frac{1}{2} \frac{\mathrm{~g}^{2}+\mathrm{f}^{2}+\mathrm{c}}{\sqrt{\mathrm{g}^{2}+\mathrm{f}^{2}}}$
(D) $\frac{1}{2} \frac{\mathrm{~g}^{2}+\mathrm{f}^{2}-\mathrm{c}}{\sqrt{\mathrm{g}^{2}+\mathrm{f}^{2}}}$
Q. 19 The area of the triangle formed by the tangents from the points $(h, k)$ to the circle $x^{2}+y^{2}=a^{2}$ and the line joining their points of contact is -
(A) $a \frac{\left(h^{2}+k^{2}-a^{2}\right)^{3 / 2}}{h^{2}+k^{2}}$
(B) $a \frac{\left(h^{2}+k^{2}-a^{2}\right)^{1 / 2}}{h^{2}+k^{2}}$
(C) $\frac{\left(\mathrm{h}^{2}+\mathrm{k}^{2}-\mathrm{a}^{2}\right)^{3 / 2}}{\mathrm{~h}^{2}+\mathrm{k}^{2}}$
(D) $\frac{\left(h^{2}+\mathrm{k}^{2}-\mathrm{a}^{2}\right)^{1 / 2}}{\mathrm{~h}^{2}+\mathrm{k}^{2}}$
Q. 20 Tangents drawn from origin to the circle $x^{2}+y^{2}-2 a x-2 b y+b^{2}=0$ are perpendicular to each other, if -
(A) $a-b=1$
(B) $a+b=1$
(C) $a^{2}=b^{2}$
(D) $a^{2}+b^{2}=1$
Q. 21 A rectangle ABCD is inscribed in a circle with a diameter lying along the line $3 y=x+10$. If A and B are the points $(-6,7)$ and $(4,7)$ respectively. Find the area of the rectangle -

(A) 40
(B) 80
(C) 20
(D) 160
Q. 22 If P is a point such that the ratio of the squares of the lengths of the tangents from $P$ to the circles $x^{2}+y^{2}+2 x-4 y-20=0$ and $x^{2}+y^{2}-4 x+2 y-44=0$ is $2: 3$ then the locus of $P$ is a circle with centre
(A) $(7,-8)$
(B) $(-7,8)$
(C) $(7,8)$
(D) $(-7,-8)$
Q. 23 Consider four circles $(x \pm 1)^{2}+(y \pm 1)^{2}=1$, then the equation of smaller circle touching these four circle is
(A) $x^{2}+y^{2}=3-\sqrt{2}$
(B) $x^{2}+y^{2}=6-3 \sqrt{2}$
(C) $x^{2}+y^{2}=5-2 \sqrt{2}$
(D) $x^{2}+y^{2}=3-2 \sqrt{2}$
Q. 24 In a system of three curves $\mathrm{C}_{1}, \mathrm{C}_{2}$ and $\mathrm{C}_{3} . \mathrm{C}_{1}$ is a circle whose equation is $x^{2}+y^{2}=4 . C_{2}$ is the locus of the point of intersection of orthogonal tangents drawn on $\mathrm{C}_{1} . \mathrm{C}_{3}$ is the locus of the point of intersection of perpendicular tangents drawn on $\mathrm{C}_{2}$. Area enclosed between the curve $\mathrm{C}_{2}$ and $\mathrm{C}_{3}$ is-
(A) $8 \pi$ sq. units
(B) $16 \pi$ sq. units
(C) $32 \pi$ sq. units
(D) None of these
Q. 25 Consider the figure and find radius of bigger circle. $\mathrm{C}_{1}$ is centre of bigger circle and radius of smaller circle is unity-

(A) $1+\sqrt{2}-\sqrt{6}$
(B) $\sqrt{2}+\sqrt{3}$
(C) $-1+\sqrt{2}+\sqrt{6}$
(D) $1+\sqrt{2}+\sqrt{6}$
Q. 26

Locus of centre of circle touching the straight lines $3 x+4 y=5$ and $3 x+4 y=20$ is -
(A) $3 x+4 y=15$
(B) $6 x+8 y=15$
(C) $3 x+4 y=25$
(D) $6 x+8 y=25$
Q. 27

If $(-3,2)$ lies on the circle $x^{2}+y^{2}+2 g x+2 f y+c=0$ which is concentric with the circle $x^{2}+y^{2}+6 x+8 y-5=0$, then $c$ is -
(A) 11
(B) -11
(C) 24
(D) None of these
Q. 28 The locus of the centre of a circle of radius 2 which rolls on the outside of the circle $x^{2}+y^{2}+3 x-6 y-9=0$ is
(A) $x^{2}+y^{2}+3 x-6 y+5=0$
(B) $x^{2}+y^{2}+3 x-6 y-31=0$
(C) $x^{2}+y^{2}+3 x-6 y+\frac{29}{4}=0$
(D) $x^{2}+y^{2}+3 x-6 y-5=0$
Q. 29 Equation of a circle whose centre is origin and radius is equal to the distance between the lines $\mathrm{x}=1$ and $x=-1$ is
(A) $x^{2}+y^{2}=1$
(B) $x^{2}+y^{2}=\sqrt{2}$
(C) $x^{2}+y^{2}=4$
(D) $x^{2}+y^{2}=-4$

## LEVEL-3

Q. 1 If the circle $x^{2}+y^{2}+2 x-4 y-k=0$ is midway between two circles
$x^{2}+y^{2}+2 x-4 y-4=0$ and
$x^{2}+y^{2}+2 x-4 y-20=0$, then $K=$
(A) 8
(B) 9
(C) 11
(D) 12
Q. 2 Equation of circle touching the lines $|x|+|y|=4$ is -
(A) $x^{2}+y^{2}=12$
(B) $x^{2}+y^{2}=16$
(C) $x^{2}+y^{2}=4$
(D) $x^{2}+y^{2}=8$
Q. 3 One possible equation of the chord of $x^{2}+y^{2}=100$ that passes through $(1,7)$ and subtends an angle $\frac{2 \pi}{3}$ at origin is -
(A) $3 y+4 x-25=0$
(B) $x+y-8=0$
(C) $3 x+4 y-31=0$
(D) None of these
Q. 4 A circle $C_{1}$ of unit radius lies in the first quadrant and touches both the co-ordinate axes. The radius of the circle which touches both the co-ordinate axes and cuts $\mathrm{C}_{1}$ so that common chord is longest -
(A) 1
(B) 2
(C) 3
(D) 4
Q. 5 From a point $P$ tangent is drawn to the circle $x^{2}+y^{2}=a^{2}$ and $a$ tangent is drawn to $x^{2}+y^{2}=b^{2}$. If these tangent are perpendicular, then locus of P is -
(A) $x^{2}+y^{2}=a^{2}+b^{2}$
(B) $x^{2}+y^{2}=a^{2}-b^{2}$
(C) $x^{2}+y^{2}=(a b)^{2}$
(D) $x^{2}+y^{2}=a+b$
Q. 6 A circle is inscribed in an equilateral triangle of side 6 . Find the area of any square inscribed in the circle -
(A) 36
(B) 12
(C) 6
(D) 9
Q. 7 The tangent at any point to the circle $x^{2}+y^{2}=r^{2}$ meets the coordinate axes at $A$ and B. If lines drawn parallel to the coordinate axes through $A$ and $B$ intersect at $P$, the locus of $P$ is
(A) $x^{2}+y^{2}=r^{-2}$
(B) $\mathrm{x}^{-2}+\mathrm{y}^{-2}=\mathrm{r}^{2}$
(C) $\frac{1}{x^{2}}+\frac{1}{y^{2}}=\frac{1}{r^{2}}$
(D) $\frac{1}{\mathrm{x}^{2}}-\frac{1}{\mathrm{y}^{2}}=\frac{1}{\mathrm{r}^{2}}$
Q. 8 If $\left(a \cos \theta_{i}, a \sin \theta_{\mathrm{i}}\right) i=1,2,3$ represent the vertices of an equilateral triangle inscribed in a circle, then -
(A) $\cos \theta_{1}+\cos \theta_{2}+\cos \theta_{3}=0$
(B) $\sin \theta_{1}+\sin \theta_{2}+\sin \theta_{3} \neq 0$
(C) $\tan \theta_{1}+\tan \theta_{2}+\tan \theta_{3}=0$
(D) $\cot \theta_{1}+\cot \theta_{2}+\cot \theta_{3}=0$
Q. 9 Of the two concentric circles the smaller one has the equation $x^{2}+y^{2}=4$. If each of the two intercepts on the line $x+y=2$ made between the two circles is 1 , the equation of the larger circle is -
(A) $x^{2}+y^{2}=5$
(B) $x^{2}+y^{2}=5+2 \sqrt{2}$
(C) $\mathrm{x}^{2}+\mathrm{y}^{2}=7+2 \sqrt{2}$
(D) $x^{2}+y^{2}=11$
Q. 10 A point on the line $\mathrm{x}=3$ from which tangent drawn to the circle $x^{2}+y^{2}=8$ are at right angles -
(A) $(3, \sqrt{7})$
(B) $(3, \sqrt{23})$
(C) $(3,-\sqrt{23})$
(D) None of these
Q. 11 If the equation of the in-circle of an equilateral triangle is $x^{2}+y^{2}+4 x-6 y+4=0$, then equation of circum-circle of the triangle is-
(A) $x^{2}+y^{2}+4 x+6 y-23=0$
(B) $x^{2}+y^{2}+4 x-6 y-23=0$
(C) $x^{2}+y^{2}-4 x-6 y-23=0$
(D) None of these
Q. 12 The angle between tangents drawn from a point $P$ to the circle $x^{2}+y^{2}+4 x-2 y-4=0$ is $60^{\circ}$. Then locus of P is -
(A) $x^{2}+y^{2}+4 x-2 y-31=0$
(B) $x^{2}+y^{2}+4 x-2 y-21=0$
(C) $x^{2}+y^{2}+4 x-2 y-11=0$
(D) $x^{2}+y^{2}+4 x-2 y=0$
Q. 13 A circle with centre A and radius 7 is tangent to the sides of an angle of $60^{\circ}$. A larger circle with centre B is tangent to the sides of the angle and to the first circle. The radius of the larger circle is

(A) $30 \sqrt{3}$
(B) 21
(C) $20 \sqrt{3}$
(D) 30

## Assertion-Reason Type Question

The following questions (Q. 14 to 23) given below consist of an "Assertion" Statement(1) and "Reason " Statement- (2) Type questions. Use the following key to choose the appropriate answer.
(A) Both Statement- (1) and Statement- (2) are true and Statement- (2) is the correct explanation of Statement- (1)
(B) Both Statement- (1) and Statement- (2) are true but Statement- (2) is not the correct explanation of Statement- (1)
(C) Statement- (1) is true but Statement- (2) is false
(D) Statement- (1) is false but Statement- (2) is true
Q. 14 Statement (1): Two points $A(10,0)$ and $\mathrm{O}(0,0)$ are given and a circle $\mathrm{x}^{2}+y^{2}-6 x+8 y-11=0$. The circle always cuts the line segments OA.
Statement (2): The centre of the circle, point A and the point $O$ are not collinear.
Q. 15 Statement (1) : If a line $L=0$ is a tangents to the circle $S=0$ then it will also be a tangent to the circle $S+\lambda L=0$.

Statement (2) : If a line touches a circles then perpendicular distance from centre of the circle on the line must be equal to the radius.
Q. 16 Consider the following statements:-

Statement (1): The circle $x^{2}+y^{2}=1$ has exactly two tangents parallel to the x -axis

Statement (2): $\frac{d y}{d x}=0$ on the circle exactly at the point $(0, \pm 1)$.
Q. 17 Statement (1): The equation of chord of the circle $x^{2}+y^{2}-6 x+10 y-9=0$, which is bisected at $(-2,4)$ must be $x+y-2=0$.
Statement (2): In notations the equation of the chord of the circle $S=0$ bisected at $\left(\mathrm{x}_{1}, \mathrm{y}_{1}\right)$ must be $\mathrm{T}=\mathrm{S}_{1}$.
Q. 18 Statement (1): If two circles
$x^{2}+y^{2}+2 g x+2 f y=0$ and $x^{2}+y^{2}+2 g^{\prime} x+2 f ' y=0$ touch each other then $f^{\prime} g=\mathrm{fg}^{\prime}$.
Statement (2) : Two circle touch each other, if line joining their centres is perpendicular to all possible common tangents.
Q. 19 Statement (1): If a circle passes through points of intersection of co-ordinate axes with the lines $\lambda x-y+1=0$ and $x-2 y+3=0$ then value of $\lambda$ is 2 .
Statement (2): If lines $a_{1} x+b_{1} y+c_{1}=0$ and $a_{2} x+b_{2} y+c_{2}=0$ intersects. Coordinate axes at concyclic points then $\frac{a_{1}}{a_{2}}=\frac{b_{1}}{b_{2}}$.
Q. 20 Statement (1): Equation of circle passing through two points $(2,0)$ and $(0,2)$ and having least area is $x^{2}+y^{2}-2 x-2 y=0$.
Statement (2): The circle of smallest radius passing through two given points $A$ and $B$ must be of radius $\frac{\mathrm{AB}}{2}$.
Q. 21 Tangents are drawn from the point $(2,3)$ to the circle $x^{2}+y^{2}=9$, then
Statement (1): Tangents are mutually
perpendicular.
Statement (2): Locus of point of intersection of perpendicular tangents is $\mathrm{x}^{2}+\mathrm{y}^{2}=18$.
Q. 22 Let ' $\theta$ ' is the angle of intersection of two circles with centres $C_{1}$ and $C_{2}$ and radius $r_{1}$ and $r_{2}$ respectively then.
Statement (1): If $\cos \theta= \pm 1$ then, the circles touch each other.
Statement (2): Two circles touch each other if $\left|\mathrm{C}_{1} \mathrm{C}_{2}\right|=\left|\mathrm{r}_{1} \pm \mathrm{r}_{2}\right|$
Q. 23 Statement (1): The locus of mid point of chords of circle $x^{2}+y^{2}=a^{2}$ which are making right angle at centre is $x^{2}+y^{2}=\frac{a^{2}}{2}$.

Statement (2): The locus of mid point of chords of circle $x^{2}+y^{2}-2 x=0$ which passes through origin is $\mathrm{x}^{2}+\mathrm{y}^{2}-\mathrm{x}=0$.

## Passage I (Question 24 to 26)

Let $\mathrm{C}_{1}, \mathrm{C}_{2}$ are two circles each of radius 1 touching internally the sides of triangles $\mathrm{POA}_{1}$, $\mathrm{PA}_{1} \mathrm{~A}_{2}$ respectively where $\mathrm{P} \equiv(0,4) \mathrm{O}$ is origin, $\mathrm{A}_{1}, \mathrm{~A}_{2}$ are the points on positive x -axis.

On the basis of above passage, answer the following questions:
Q. 24 Angle subtended by circle $\mathrm{C}_{1}$ at P is-
(A) $\tan ^{-1} \frac{2}{3}$
(B) $2 \tan ^{-1} \frac{2}{3}$
(C) $\tan ^{-1} \frac{3}{4}$
(D) $2 \tan ^{-1} \frac{3}{4}$
Q. 25 Centre of circle $\mathrm{C}_{2}$ is-
(A) $(3,1)$
(B) $\left(3 \frac{1}{2}, 1\right)$
(C) $\left(3 \frac{3}{4}, 1\right)$
(D) None of these
Q. 28 Equation of circle passing through A and B whose AB is diameter-
(A) $x^{2}+y^{2}-3 x-3 y-5=0$
(B) $x^{2}+y^{2}-3 x-3 y-4=0$
(C) $x^{2}+y^{2}+3 x+3 y-4=0$
(D) $x^{2}+y^{2}+3 x+3 y-5=0$
Q. 29 Mid point of AB is-
(A) $\left(\frac{5}{2}, \frac{1}{2}\right)$
(B) $\left(\frac{3}{2}, \frac{3}{2}\right)$
(C) $(2,1)$
(D) $(1,2)$

## Passage-III (Question 30 to 31)

To the circle $x^{2}+y^{2}=4$ two tangents are drawn from $\mathrm{P}(-4,0)$, which touches the circle at A and B and a rhombus PA $\mathrm{P}^{\prime} \mathrm{B}$ is completed.
On the basis of above passage, answer the following questions :
Q. 30 Circumcentre of the triangle PAB is at
(A) $(-2,0)$
(B) $(2,0)$
(C) $\left(\frac{\sqrt{3}}{2}, 0\right)$
(D) None of these
Q. 31 Ratio of the area of triangle $\mathrm{PAP}^{\prime}$ to that of $\mathrm{P}^{\prime} \mathrm{AB}$ is
(A) $2: 1$
(B) $1: 2$
(C) $\sqrt{3}: 2$
(D) None of these
Q. 26 Length of tangent from $P$ to circle $\mathrm{C}_{2^{-}}$
(A) 4
(B) $\frac{9}{2}$
(C) 5
(D) $\frac{19}{4}$

## Passage II (Question 27 to 29)

Two circles $S_{1}: x^{2}+y^{2}-2 x-2 y-7=0$ and $S_{2}: x^{2}+y^{2}-4 x-4 y-1=0$ intersects each other at A and B.
On the basis of above passage, answer the following questions:
Q. 27 Length of AB is-
(A) 6
(B) $\sqrt{33}$
(C) $\sqrt{34}$
(D) $\sqrt{35}$

## LEVEL- 4

(Question asked in previous AIEEE and IIT-JEE)

## Section -A

Q. 1 The square of the length of tangent from (3, -4) on the circle $x^{2}+y^{2}-4 x-6 y+3=0-$
[AIEEE-2002]
(A) 20
(B) 30
(C) 40
(D) 50
Q. 2 If the two circles $(x-1)^{2}+(y-3)^{2}=r^{2}$ and $x^{2}+y^{2}-8 x+2 y+8=0$ intersect in two distinct points, then
[AIEEE-2003]
(A) $r>2$
(B) $2<\mathrm{r}<8$
(C) $\mathrm{r}<2$
(D) $r=2$
Q. 3 The lines $2 x-3 y=5$ and $3 x-4 y=7$ are diameters of a circle having area as 154 sq. units. Then the equation of the circle is -
[AIEEE-2003]
(A) $x^{2}+y^{2}-2 x+2 y=62$
(B) $x^{2}+y^{2}+2 x-2 y=62$
(C) $x^{2}+y^{2}+2 x-2 y=47$
(D) $x^{2}+y^{2}-2 x+2 y=47$
Q. 4 If a circle passes through the point $(a, b)$ and cuts the circle $x^{2}+y^{2}=4$ orthogonally, then the locus of its centre is-
[AIEEE-2004]
(A) $2 a x+2 b y+\left(a^{2}+b^{2}+4\right)=0$
(B) $2 a x+2 b y-\left(a^{2}+b^{2}+4\right)=0$
(C) $2 a x-2 b y+\left(a^{2}+b^{2}+4\right)=0$
(D) $2 a x-2 b y-\left(a^{2}+b^{2}+4\right)=0$
Q. 5 A variable circle passes through the fixed point $A(p, q)$ and touches $x$ - axis. The locus of the other end of the diameter through A is-
[AIEEE-2004]
(A) $(x-p)^{2}=4 q y$
(B) $(x-q)^{2}=4 p y$
(C) $(y-p)^{2}=4 q x$
(D) $(y-q)^{2}=4 p x$
Q. 6 If the lines $2 x+3 y+1=0$ and $3 x-y-4=0$ lie along diameters of a circle of circumference $10 \pi$, then the equation of the circle is-
[AIEEE-2004]
(A) $x^{2}+y^{2}-2 x+2 y-23=0$
(B) $x^{2}+y^{2}-2 x-2 y-23=0$
(C) $x^{2}+y^{2}+2 x+2 y-23=0$
(D) $x^{2}+y^{2}+2 x-2 y-23=0$
Q. 7 If the circles $x^{2}+y^{2}+2 a x+c y+a=0$ and $x^{2}+y^{2}-3 a x+d y-1=0$ intersect in two distinct point $P$ and $Q$ then the line $5 x+b y-a=0$ passes through $P$ and $Q$ for -
[AIEEE-2005]
(A) exactly one value of a
(B) no value of a
(C) infinitely many values of a
(D) exactly two values of a
Q. 8 A circle touches the x -axis and also touches the circle with centre at $(0,3)$ and radius 2 . The locus of the centre of the circle is-
[AIEEE-2005]
(A) an ellipse
(B) a circle
(C) a hyperbola
(D) a parabola
Q. 9 If a circle passes through the point $(a, b)$ and cuts the circle $x^{2}+y^{2}=p^{2}$ orthogonally, then the equation of the locus of its centre is -
[AIEEE-2005]
(A) $\mathrm{x}^{2}+\mathrm{y}^{2}-3 a \mathrm{x}-4 \mathrm{by}+\left(\mathrm{a}^{2}+\mathrm{b}^{2}-\mathrm{p}^{2}\right)=0$
(B) $2 \mathrm{ax}+2 \mathrm{by}-\left(\mathrm{a}^{2}-\mathrm{b}^{2}+\mathrm{p}^{2}\right)=0$
(C) $x^{2}+y^{2}-2 a x-3 b y+\left(a^{2}-b^{2}-p^{2}\right)=0$
(D) $2 a x+2 b y-\left(a^{2}+b^{2}+p^{2}\right)=0$
Q. 10 If the pair of lines $a x^{2}+2(a+b) x y+b y^{2}=0$ lie along diameters of a circle and divide the circle into four sectors such that the area of one of the sectors is thrice the area of another sector then -
[AIEEE-2005]
(A) $3 \mathrm{a}^{2}-10 \mathrm{ab}+3 \mathrm{~b}^{2}=0$
(B) $3 a^{2}-2 a b+3 b^{2}=0$
(C) $3 \mathrm{a}^{2}+10 \mathrm{ab}+3 \mathrm{~b}^{2}=0$
(D) $3 a^{2}+2 a b+3 b^{2}=0$
Q. 11 If the lines $3 x-4 y-7=0$ and $2 x-3 y-5=0$ are two diameters of a circle of area $49 \pi$ square units, the equation of the circle is-
[AIEEE-2006]
(A) $x^{2}+y^{2}+2 x-2 y-62=0$
(B) $x^{2}+y^{2}-2 x+2 y-62=0$
(C) $x^{2}+y^{2}-2 x+2 y-47=0$
(D) $x^{2}+y^{2}+2 x-2 y-47=0$
Q. 12 Let C be the circle with centre $(0,0)$ and radius 3 units. The equation of the locus of the mid points of the chords of the circle $C$ that subtend an angle of $\frac{2 \pi}{3}$ at its centre is - [AIEEE-2006]
(A) $x^{2}+y^{2}=1$
(B) $x^{2}+y^{2}=\frac{27}{4}$
(C) $x^{2}+y^{2}=\frac{9}{4}$
(D) $x^{2}+y^{2}=\frac{3}{2}$
Q. 13 Consider a family of circles which are passing through the point $(-1,1)$ and are tangent to x -axis. If $(\mathrm{h}, \mathrm{k})$ are the co-ordinates of the centre of the circles, then the set of values of k is given by the interval-
[AIEEE-2007]
(A) $0<\mathrm{k}<1 / 2$
(B) $\mathrm{k} \geq 1 / 2$
(C) $-1 / 2 \leq \mathrm{k} \leq 1 / 2$
(D) $\mathrm{k} \leq 1 / 2$
Q. 14 The point diametrically opposite to the point $P(1,0)$ on the circle $x^{2}+y^{2}+2 x+4 y-3=0$ is -
[AIEEE-2008]
(A) $(-3,4)$
(B) $(-3,-4)$
(C) $(3,4)$
(D) $(3,-4)$
Q. 15 If P and Q are the points of intersection of the circles $x^{2}+y^{2}+3 x+7 y+2 p-5=0$ and $x^{2}+y^{2}+2 x+2 y-p^{2}=0$, then there is a circle passing through $\mathrm{P}, \mathrm{Q}$, and $(1,1)$ for-
[AIEEE- 2009]
(A) All except one value of p
(B) All except two values of $p$
(C) Exactly one value of $p$
(D) All values of p
Q. 16 The circle $x^{2}+y^{2}=4 x+8 y+5$ intersects the line $3 x-4 y=m$ at two distinct points if -
[AIEEE- 2010]
(A) $-85<\mathrm{m}<-35$
(B) $-35<$ m $<15$
(C) $15<\mathrm{m}<65$
(D) $35<\mathrm{m}<85$
Q. 17 The two circles $x^{2}+y^{2}=a x$ and $x^{2}+y^{2}=c^{2}(c>0)$ touch each other if -
[AIEEE- 2011]
(A) $2|a|=c$
(B) $|\mathrm{a}|=\mathrm{c}$
(C) $\mathrm{a}=2 \mathrm{c}$
(D) $|\mathrm{a}|=2 \mathrm{c}$
Q. 18 The equation of the circle passing through the point $(1,0)$ and $(0,1)$ and having the smallest radius is -
[AIEEE- 2011]
(A) $x^{2}+y^{2}-2 x-2 y+1=0$
(B) $x^{2}+y^{2}-x-y=0$
(C) $x^{2}+y^{2}+2 x+2 y-7=0$
(D) $x^{2}+y^{2}+x+y-2=0$
Q. 19 The length of the diameter of the circle which touches the x -axis at the point $(1,0)$ and passes through the point $(2,3)$ is :
[AIEEE-2012]
(A) $3 / 5$
(B) $6 / 5$
(C) $5 / 3$
(D) $10 / 3$
Q. 20 The circle passing through $(1,-2)$ and touching the axis of x at $(3,0)$ also passes through the point -
[JEE Main - 2013]
(A) $(5,-2)$
(B) $(-2,5)$
(C) $(-5,2)$
(D) $(2,-5)$

## Section -B

Q. 1 The centre of the circle passing through points $(0,0),(1,0)$ and touching the circle $x^{2}+y^{2}=9$ is
[IIT-1992]
(A) $(3 / 2,1 / 2)$
(B) $(1 / 2,3 / 2)$
(C) $(1 / 2,1 / 2)$
(D) $\left(1 / 2,-2^{1 / 2}\right)$
Q. 2 The equation of the circle which touches both the axes and the straight line $4 x+3 y=6$ in the first quadrant and lies below it is-
[IIT-1992]
(A) $4 x^{2}+4 y^{2}-4 x-4 y+1=0$
(B) $x^{2}+y^{2}-6 x-6 y+9=0$
(C) $x^{2}+y^{2}-6 x-y+9=0$
(D) $4\left(x^{2}+y^{2}-x-6 y\right)+1=0$
Q. 3 The slope of the tangent at the point (h, h) of the circle $x^{2}+y^{2}=a^{2}$ is -
[IIT-1993]
(A) 0
(B) 1
(C) -1
(D) depends on $h$
Q. 4 The intercept on the line $y=x$ by the circle $x^{2}+y^{2}-2 x=0$ is $A B$. Equation of the circle with $A B$ as a diameter is-
[IIT-96/AIEEE -04]
(A) $x^{2}+y^{2}+x+y=0$
(B) $-x^{2}+y^{2}+x-y=0$
(C) $x^{2}+y^{2}-x-y=0$
(D) None of these
Q. 5 If a circle passes thro' the points of intersection of the co - ordinate axes with the lines $\lambda x-y+1=0$ and $x-2 y+3=0$, then the value of $\lambda$ is-
[IIT-1997]
(A) 2
(B) 4
(C) 6
(D) 3
Q. 6 The number of common tangents to the circles $x^{2}+y^{2}=4$ and $x^{2}+y^{2}-6 x-8 y=24$ is
[IIT-1998]
(A) 0
(B) 1
(C) 3
(D) 4
Q. 7 Let $L_{1}$ be a straight line passing through the origin and $L_{2}$ be the straight line $x+y=1$. If the intercepts made by the circle $x^{2}+y^{2}-x+3 y=0$ on $L_{1}$ and $L_{2}$ are equal, then which of the following equations can represent $\mathrm{L}_{1}$ -
[IIT-1999]
(A) $x+y=0$
(B) $x-y=0$
(C) $x+7 y=0$
(D) None of these
Q. 8 If the circles $x^{2}+y^{2}+2 x+2 k y+6=0$ and $x^{2}+y^{2}+2 k y+k=0$ intersect orthogonally, then k is -
[IIT-2000]
(A) 2 or $-3 / 2$
(B) -2 or $-3 / 2$
(C) 2 or $3 / 2$
(D) -2 or $3 / 2$
Q. 9 The triangle PQR is inscribed in the circle $x^{2}+y^{2}=25$. If $Q$ and $R$ have co-ordinates $(3,4)$ and $(-4,3)$ respectively, then angle QPR is equal to -
[IIT-2000]
(A) $\pi / 2$
(B) $\pi / 3$
(C) $\pi / 4$
(D) $\pi / 6$
Q. 10 Let PQ and RS be tangents at the extremities of the diameter PR of a circle of radius r. If PS and RQ intersect at a point $X$ on the circumference of the circle, then 2 r equals
[IIT-2001]
(A) $\sqrt{\text { PQ.RS }}$
(B) $\frac{P Q+R S}{2}$
(C) $\frac{2 P Q \cdot R S}{P Q+R S}$
(D) $\sqrt{\frac{\mathrm{PQ}^{2}+\mathrm{RS}^{2}}{2}}$
Q. 11 If the tangent at the point P on the circle $x^{2}+y^{2}+6 x+6 y=2$ meets the straight line $5 x-2 y+6=0$ at a point $Q$ on the $y$-axis, then the length of PQ is -
[IIT-2002]
(A) 4
(B) 2
(C) 5
(D) 3
Q. 12 If $\mathrm{a}>2 \mathrm{~b}>0$ then the positive value of m for which $y=m x-b \sqrt{1+m^{2}}$ is a common tangent to $x^{2}+y^{2}=b^{2}$ and $(x-a)^{2}+y^{2}=b^{2}$ is -
[IIT-2002]
(A) $\frac{2 b}{\sqrt{a^{2}-4 b^{2}}}$
(B) $\frac{\sqrt{a^{2}-4 b^{2}}}{2 b}$
(C) $\frac{2 b}{a-2 b}$
(D) $\frac{b}{a-2 b}$
Q. 13 Diameter of the given circle $x^{2}+y^{2}-2 x-6 y+6=0$ is the chord of another circle C having centre $(2,1)$, the radius of the circle $C$ is- [IIT 2004]
(A) $\sqrt{3}$
(B) 2
(C) 3
(D) 1
Q. 14 Locus of the centre of circle touching to the x -axis \& the circle $\mathrm{x}^{2}+(\mathrm{y}-1)^{2}=1$ externally is -
[IIT-2005]
(A) $\{(0, \mathrm{y}) ; \mathrm{y} \leq 0\} \cup\left(\mathrm{x}^{2}=4 \mathrm{y}\right)$
(B) $\{(0, \mathrm{y}) ; \mathrm{y} \leq 0\} \cup\left(\mathrm{x}^{2}=\mathrm{y}\right)$
(C) $\{(\mathrm{x}, \mathrm{y}) ; \mathrm{y} \leq \mathrm{y}\} \cup\left(\mathrm{x}^{2}=4 \mathrm{y}\right)$
(D) $\{(0, y) ; y \geq 0\} \cup\left(x^{2}+(y-1)^{2}=4\right.$
Q. 15 Tangents are drawn from the point $(17,7)$ to the circle $x^{2}+y^{2}=169$.
[IIT 2007]
STATEMENT-1: The tangents are mutually perpendicular.

## Because

STATEMENT-2: The locus of the points from which mutually perpendicular tangents can be drawn to given circle is $\mathrm{x}^{2}+\mathrm{y}^{2}=338$.
(A) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(B) Statement-1, is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(C) Statement-1 is True, Statement-2 is False
(D) Statement-1 is False, Statement-2 is True
Q. 16 Tangents drawn from the point $\mathrm{P}(1,8)$ to the circle $x^{2}+y^{2}-6 x-4 y-11=0$ touch the circle at the points A and B . The equation of the circumcircle of the triangle PAB is - [IIT-2009]
(A) $x^{2}+y^{2}+4 x-6 y+19=0$
(B) $x^{2}+y^{2}-4 x-10 y+19=0$
(C) $x^{2}+y^{2}-2 x+6 y-29=0$
(D) $x^{2}+y^{2}-6 x-4 y+19=0$
Q. 17 The centres of two circles $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ each of unit radius are at a distance of 6 units from each other. Let P be the mid point of the line segment joining the centres of $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ and C be a circle touching circles $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ externally. If a common tangent to $\mathrm{C}_{1}$ and C passing through P is also a common tangent to $\mathrm{C}_{2}$ and C , then the radius of the circle C is-
(A) 8
(B) 4
(C) 16
(D) 2
[IIT 2009]
Q. 18 The circle passing through the point $(-1,0)$ and touching the $y$-axis at $(0,2)$ also passes through the point -
[IIT 2011]
(A) $\left(-\frac{3}{2}, 0\right)$
(B) $\left(-\frac{5}{2}, 2\right)$
(C) $\left(-\frac{3}{2}, \frac{5}{2}\right)$
(D) $(-4,0)$
Q. 19 The straight line $2 x-3 y=1$ divides the circular region $x^{2}+y^{2} \leq 6$ into two parts. If $S=\left\{\left(2, \frac{3}{4}\right),\left(\frac{5}{2}, \frac{3}{4}\right),\left(\frac{1}{4},-\frac{1}{4}\right),\left(\frac{1}{8}, \frac{1}{4}\right)\right\}$, then the number of point(s) in $S$ lying inside the smaller part is -
[IIT 2011]
(A) 8
(B) 2
(C) 4
(D) 16
Q. 23 Circle(s) touching $x$-axis at a distance 3 from the origin and having an intercept of length $2 \sqrt{7}$ on $y$-axis is (are) -
[JEE - Advance 2013]
(A) $x^{2}+y^{2}-6 x+8 y+9=0$
(B) $x^{2}+y^{2}-6 x+7 y+9=0$
(C) $x^{2}+y^{2}-6 x-8 y+9=0$
(D) $x^{2}+y^{2}-6 x-7 y+9=0$

## Paragraph for Questions 21 and 22

A tangent PT is drawn to the circle $\mathrm{x}^{2}+\mathrm{y}^{2}=4$ at the point $\mathrm{P}(\sqrt{3}, 1)$. A straight line L , perpendicular to PT is a tangent to the circle $(x-3)^{2}+y^{2}=1$.
[IIT 2012]
Q. 21 A possible equation of $L$ is
(A) $x-\sqrt{3} y=1$
(B) $x+\sqrt{3} y=1$
(C) $x-\sqrt{3} y=-1$
(D) $x+\sqrt{3} y=5$
Q. 22 A common tangent of the two circles is
(A) $x=4$
(B) $y=2$
(C) $x+\sqrt{3} y=4$
(D) $x+2 \sqrt{2} y=6$

## ANSWER KEY

LEVEL- 1

| Qus. | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ans. | D | D | A | B | B | A | A | A | C | C | C | D | C | A | B | C | D | A | B | C |
| Qus. | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | $\mathbf{2 5}$ | $\mathbf{2 6}$ | $\mathbf{2 7}$ | $\mathbf{2 8}$ | $\mathbf{2 9}$ | $\mathbf{3 0}$ | $\mathbf{3 1}$ | $\mathbf{3 2}$ | $\mathbf{3 3}$ | $\mathbf{3 4}$ | $\mathbf{3 5}$ | $\mathbf{3 6}$ | $\mathbf{3 7}$ | $\mathbf{3 8}$ | $\mathbf{3 9}$ | $\mathbf{4 0}$ |
| Ans. | D | B | B | C | B | A | D | A | B | C | B | C | D | A | C | A | B | B | C | A |
| Qus. | $\mathbf{4 1}$ | $\mathbf{4 2}$ | $\mathbf{4 3}$ | $\mathbf{4 4}$ | $\mathbf{4 5}$ | $\mathbf{4 6}$ | $\mathbf{4 7}$ | $\mathbf{4 8}$ | $\mathbf{4 9}$ | $\mathbf{5 0}$ | $\mathbf{5 1}$ | $\mathbf{5 2}$ | $\mathbf{5 3}$ | $\mathbf{5 4}$ | $\mathbf{5 5}$ | $\mathbf{5 6}$ | $\mathbf{5 7}$ | $\mathbf{5 8}$ | $\mathbf{5 9}$ | $\mathbf{6 0}$ |
| Ans. | D | A | B | A | B | A | C | A | A | C | B | C | C | C | C | C | A | C | D | A |
| Qus. | $\mathbf{6 1}$ | $\mathbf{6 2}$ | $\mathbf{6 3}$ | $\mathbf{6 4}$ | $\mathbf{6 5}$ | $\mathbf{6 6}$ | $\mathbf{6 7}$ | $\mathbf{6 8}$ | $\mathbf{6 9}$ | $\mathbf{7 0}$ | $\mathbf{7 1}$ | $\mathbf{7 2}$ | $\mathbf{7 3}$ | $\mathbf{7 4}$ | $\mathbf{7 5}$ | $\mathbf{7 6}$ | $\mathbf{7 7}$ | $\mathbf{7 8}$ | $\mathbf{7 9}$ | $\mathbf{8 0}$ |
| Ans. | B | A | B | A | A | A | D | B | C | C | D | B | B | B | D | D | B | C | B | D |
| Qus. | $\mathbf{8 1}$ | $\mathbf{8 2}$ | $\mathbf{8 3}$ | $\mathbf{8 4}$ | $\mathbf{8 5}$ | $\mathbf{8 6}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Ans. | C | C | B | C | C | C |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## LEVEL- 2

| Qus. | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ans. | B | A | A | D | A | B | B | A | A | B | C | C | A | A | C | B | B | D | A | C |
| Qus. | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | $\mathbf{2 5}$ | $\mathbf{2 6}$ | $\mathbf{2 7}$ | $\mathbf{2 8}$ | $\mathbf{2 9}$ |  |  |  |  |  |  |  |  |  |  |  |
| Ans. | B | B | D | A | D | D | B | B | C |  |  |  |  |  |  |  |  |  |  |  |

LEVEL- 3

| Qus. | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ans. | C | D | A | C | A | C | C | A | B | A | B | A | B | B | B | A | D | C | C | A |
| Qus. | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | $\mathbf{2 5}$ | $\mathbf{2 6}$ | $\mathbf{2 7}$ | $\mathbf{2 8}$ | $\mathbf{2 9}$ | $\mathbf{3 0}$ | $\mathbf{3 1}$ |  |  |  |  |  |  |  |  |  |
| Ans. | D | A | B | C | B | B | C | B | B | A | D |  |  |  |  |  |  |  |  |  |

## LEVEL- 4

## SECTION-A

| Qus. | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ans. | C | B | D | B | A | A | B | D | D | D | C | C | B | B | A | B | B | B | D | A |

## SECTION-B

1.[D]


$$
\Rightarrow \mathrm{C}_{1} \mathrm{C}_{2}=\left|\mathrm{r}_{1}-\mathrm{r}_{2}\right|
$$

Clearly x -coordinate $=\frac{1}{2}$ then y -coordinate

$$
=\sqrt{\left(\frac{3}{2}\right)^{2}-\frac{1}{4}}=\sqrt{\frac{9}{4}-\frac{1}{4}}=\sqrt{\frac{8}{4}}= \pm \sqrt{2}
$$

2.[A] $\quad(x-h)^{2}+(y-h)^{2}=h^{2}$
$\Rightarrow \mathrm{x}^{2}+\mathrm{y}^{2}-2 \mathrm{hx}-2 \mathrm{hy}+\mathrm{h}^{2}=0$
Also $4 x+3 y=6$ touches the circle then
$\left|\frac{4 h+3 h-6}{5}\right|=\mathrm{h} \Rightarrow 7 \mathrm{~h}-6= \pm 5 \mathrm{~h}$
$\Rightarrow \mathrm{h}=3$ and $\mathrm{h}=\frac{1}{2}$
Then equation
$x^{2}+y^{2}-6 x-6 y+9=0$ and
$4 x^{2}+4 y^{2}-4 x-4 y+1=0$
3.[C] Equation of tangent
$h x+h y=a^{2}$
Slope is -1 .
4. [C]


Centre of required circle is $\left(\frac{1}{2}, \frac{1}{2}\right)$
Radius $=\frac{1}{\sqrt{2}}$
Hence equation is $x^{2}+y^{2}-x-y=0$
5.[A] $\quad \lambda=2\left(\right.$ as a $\left._{1} \mathrm{a}_{2}=\mathrm{b}_{1} \mathrm{~b}_{2}\right)$
6.[B] As these two circles touch each other internally.
7.[C, B] $\mathrm{L}_{1}: \mathrm{y}-\mathrm{mx}=0$
$\mathrm{L}_{2}: \mathrm{x}+\mathrm{y}=1$
Intercept made by $\mathrm{L}_{1}$
$=2 \sqrt{\frac{1}{4}+\frac{9}{4}-\frac{(\mathrm{m} \cdot 1 / 2+3 / 2)^{2}}{\left(1+\mathrm{m}^{2}\right)}}=\sqrt{10-\frac{(\mathrm{m}+3)^{2}}{1+\mathrm{m}^{2}}}$
Intercept made by $L_{2}$
$=2 \sqrt{\frac{10}{4}-\left(\frac{1 / 2-3 / 2-1}{\sqrt{2}}\right)^{2}}=\sqrt{10-\frac{16}{2}}=\sqrt{10-8}=\sqrt{2}$
As these two are equal
$10-\frac{(\mathrm{m}+3)^{2}}{1+\mathrm{m}^{2}}=2$
$\Rightarrow \frac{(\mathrm{m}+3)^{2}}{1+\mathrm{m}^{2}}=8 \Rightarrow \mathrm{~m}^{2}+6 \mathrm{~m}+9=8 \mathrm{~m}^{2}+8$
$\Rightarrow 7 \mathrm{~m}^{2}-6 \mathrm{~m}-1=0$
$\Rightarrow \mathrm{m}=\frac{6 \pm \sqrt{36+28}}{14}=\frac{6 \pm 8}{14}=1,-\frac{1}{7}$
Hence equations are $y=x \& x+7 y=0$
8. [A] (2) (1) (0) + (2) (k) $(\mathrm{k})=6+\mathrm{k}$
$\Rightarrow 2 \mathrm{k}^{2}-\mathrm{k}-6=0$
$\Rightarrow \mathrm{k}=\frac{1 \pm \sqrt{1+48}}{4}=\frac{1 \pm 7}{4}=2,-\frac{3}{2}$
9.[C]


Slope of OQ $=\frac{4}{3}$
Slope of $\mathrm{OR}=\frac{3}{-4}$
As product of these slopes is -1 OQ is perpendicular to OR.
Hence $\angle \mathrm{QPR}=\frac{\pi}{4}$
10.[A]

$\tan \theta=\frac{\mathrm{RS}}{\mathrm{PR}}=\frac{\mathrm{RS}}{2 \mathrm{r}}$
$\mathrm{RS}=2 \mathrm{r} \tan \theta$
Also, $\tan (90-\theta)=\frac{P Q}{2 r}$
$P Q=2 r \cot \theta$
$\therefore 4 r^{2}=P Q . R S \Rightarrow 2 r=\sqrt{P Q . R S}$
11.[C] Line $5 x-2 y+6=0$ intersect $y$-axis at $(0,3)$
then length of tangent $P Q=\sqrt{9+18-2}=5$
12.[A] $\mathrm{y}=\mathrm{mx}-\mathrm{b} \sqrt{1+\mathrm{m}^{2}}$
$\Rightarrow m x-y-b \sqrt{1+\mathrm{m}^{2}}=0$
$\mathrm{b}=\left|\frac{\mathrm{ma}-\mathrm{b} \sqrt{1+\mathrm{m}^{2}}}{\sqrt{1+\mathrm{m}^{2}}}\right|$
$\left(1+\mathrm{m}^{2}\right) \mathrm{b}^{2}=\left(\mathrm{ma}-\mathrm{b} \sqrt{1+\mathrm{m}^{2}}\right)^{2}$
$b^{2}+m^{2} b^{2}=m^{2} a^{2}+b^{2}\left(1+m^{2}\right)-2 m a b \sqrt{1+m^{2}}$
$\Rightarrow \mathrm{b}^{2}=\mathrm{m}^{2} \mathrm{a}^{2}+\mathrm{b}^{2}-2 \mathrm{mab} \sqrt{1+\mathrm{m}^{2}}$
$\Rightarrow \mathrm{ma}\left(\mathrm{ma}-2 \mathrm{~b} \sqrt{1+\mathrm{m}^{2}}\right)=0$
$\Rightarrow \mathrm{m}=0$ or $\frac{\mathrm{m}^{2} \mathrm{a}^{2}}{4 \mathrm{~b}^{2}}=1+\mathrm{m}^{2}$
$\Rightarrow \mathrm{m}^{2}\left(\frac{\mathrm{a}^{2}-4 \mathrm{~b}^{2}}{4 \mathrm{~b}^{2}}\right)=1 \Rightarrow \mathrm{~m}= \pm \frac{2 \mathrm{~b}}{\sqrt{\mathrm{a}^{2}-4 \mathrm{~b}^{2}}}$
13.[C]

$r^{2}=1+4+4$
$\Rightarrow r^{2}=9 \Rightarrow r=3$
14.[A]

$\sqrt{\mathrm{h}^{2}+(\mathrm{k}-1)^{2}}=1+\mathrm{k}$
$\Rightarrow \mathrm{h}^{2}+\mathrm{k}^{2}-2 \mathrm{k}+1=1+2 \mathrm{k}+\mathrm{k}^{2}$
$\Rightarrow \mathrm{h}^{2}=4 \mathrm{k}$
$\Rightarrow x^{2}=4 y$
Required locus $\{(0, y): y \leq 0\} \cup\left(x^{2}=4 y\right)$
15.[A] As $(17,7)$ lies on the director circle
$x^{2}+y^{2}=338$
16.[B] Equation of line $A B$ is
$\mathrm{x}+8 \mathrm{y}-3(\mathrm{x}+1)-2(\mathrm{y}+8)-11=0$
$\Rightarrow-2 x+6 y-30=0$
$\Rightarrow x-3 y+15=0$
Equation of circle passes through $A \& B$ is given by $\left(x^{2}+y^{2}-6 x-4 y-11\right)+\lambda(x-3 y+15)$ $=0$
As, $(3,2)$ will lie on it $-24+12 \lambda=0$
$\lambda=2$
Hence equation is $x^{2}+y^{2}-4 x-10 y+19=0$
17.[A]


In $\triangle \mathrm{APR}$
$\cos \theta=\frac{1}{3}$
Now in $\triangle \mathrm{APQ}$
$\sin (90-\theta)=\frac{A P}{A Q}$
$\Rightarrow \cos \theta=\frac{3}{\mathrm{AQ}}$
$\Rightarrow \frac{1}{3}=\frac{3}{\mathrm{AQ}}$
$\Rightarrow A Q=9$
Hence $\mathrm{r}=9-1=8$
18.[D]

$\therefore \quad(\mathrm{h}-0)^{2}+(2-2)^{2}=(\mathrm{h}+1)^{2}+(2-0)^{2}$
$h^{2}=h^{2}+1+2 h+4$
$\mathrm{h}=-5 / 2$
equation of circle is
$\left(x+\frac{5}{2}\right)^{2}+(y-2)^{2}=\left(-\frac{5}{2}-0\right)^{2}$
$x^{2}+\frac{25}{4}+5 x+y^{2}+4-4 y=\frac{25}{4}$
$x^{2}+y^{2}+5 x-4 y+4=0$
from given points only point $(-4,0)$ satisfies this equation
19.[B]


Point ( $\mathrm{x}_{1} \mathrm{y}_{1}$ ) lies inside the region if $\mathrm{x}_{1}^{2}+\mathrm{y}_{1}^{2}-6 \leq 0$ and $2 \mathrm{x}_{1}-3 \mathrm{y}_{1}-1 \leq 0$
$P_{1}\left(2, \frac{3}{4}\right) \quad 4+\frac{9}{16}-6 \leq 0 \quad$ True $4-\frac{9}{4}-1>0 \quad$ True
$\mathrm{P}_{2}\left(\frac{5}{2}, \frac{3}{4}\right) \quad \frac{25}{4}+\frac{9}{16}-6 \leq 0 \quad$ False
$\mathrm{P}_{3}\left(\frac{1}{4},-\frac{1}{4}\right) \quad \frac{1}{16}+\frac{1}{16}-6 \leq \square 0 \quad$ True $\frac{2}{4}+\frac{3}{4}-1>0 \quad$ True
$\mathrm{P}_{4}\left(\frac{1}{8}, \frac{1}{4}\right) \quad \frac{1}{64}+\frac{1}{16}-6 \leq 0 \quad$ True
$\frac{2}{8}-\frac{3}{4}-1>0 \quad$ False
So $P_{1}$ and $P_{2}$ lies in the interval.
20.[A]


Equation of chord AB is $\mathrm{T}=0$
$\alpha x+\left(\frac{4 \alpha-20}{5}\right) y=9$
$\& h x+k y-9=h^{2}+k^{2}-9$
$\because$ Equation (i) \& (ii) both represent the same line
So $\frac{\alpha}{\mathrm{h}}=\frac{\frac{4 \alpha-20}{5}}{\mathrm{k}}=\frac{9}{\mathrm{~h}^{2}+\mathrm{k}^{2}}$
$\alpha=\frac{9 \mathrm{~h}}{\mathrm{~h}^{2}+\mathrm{k}^{2}}=\frac{45 \mathrm{k}+20\left(\mathrm{~h}^{2}+\mathrm{k}^{2}\right)}{4\left(\mathrm{~h}^{2}+\mathrm{k}^{2}\right)}$
$36 \mathrm{~h}=45 \mathrm{k}+20\left(\mathrm{~h}^{2}+\mathrm{k}^{2}\right)$
$20\left(x^{2}+y^{2}\right)-36 x+45 y=0$
21.[A]


Slope of $\mathrm{PT}=\tan \left(120^{\circ}\right)=-\sqrt{3}$
Slope of line $\mathrm{L}=\frac{1}{\sqrt{3}}$
Line $L \equiv x-\sqrt{3} y+\lambda=0$
tangent to $(x-3)^{2}+y^{2}=1$

$$
\frac{|3+\lambda|}{2}=1
$$

$\lambda+3=2,-2$
$\lambda=-1,-5$
$x-\sqrt{3} y-1=0$
or $\quad x-\sqrt{3} y-5=0$
22.[D] Common tangent both circles


So $P \equiv(6,0)$
line through $P$
$\lambda x-y-6 \lambda=0$
tangent to circle $\frac{|3 \lambda|}{\sqrt{1+\lambda^{2}}}=1$
$9 \lambda^{2}=1+\lambda^{2} \Rightarrow \lambda^{2}=\frac{1}{8}$
$\lambda=\frac{1}{2 \sqrt{2}}, \frac{-1}{2 \sqrt{2}}$
Equation of tangent $x+2 \sqrt{2} y=6$

## 23.[A, C]


$\mathrm{k}=\sqrt{9+7}=4$
Circle is
$(x-3)^{2}+(y-4)^{2}=16$
$x^{2}+y^{2}-6 x-8 y+9=0$
or
$(x+3)^{2}+(y-4)^{2}=16$
$x^{2}+y^{2}+6 x-8 y+9=0$
or
$(x-3)^{2}+(y+4)^{2}=16$ which is option (A).

